



Federal Board SSC-I Examination Mathematics Model Question Paper (Science Group) (Curriculum 2006)

Section A(Marks 15)

Q1.

Part No.	1	2	3	4	5	6	7
Correct Option	D	B	A	A	B	B	A

8	9	10	11	12	13	14	15
B	D	B	B	B	D	A	A

Section B(Marks 4x9=36)

Q. 2 Attempt any nine parts from the following. All parts carry equal marks ((9*4=36)

i. if $A = \begin{bmatrix} 1 & 7 \\ 4 & 2 \\ 2 & 2 \end{bmatrix}$

- find $|A|$
- is matrix A nonsingular?
- Find A^{-1} (multiplicative inverse)

Sol.

a) $|A| = \begin{vmatrix} 1 & 7 \\ 4 & 2 \\ 2 & 2 \end{vmatrix}$
 $= \frac{1}{4} \times 2 - \frac{7}{2} \times 2$
 $= \frac{1}{2} - 7$
 $= \frac{1-14}{2}$
 $= -\frac{13}{2}$

1 mark

b) $|A| = \frac{13}{2} \neq 0$ so matrix A is nonsingular.

1 mark

c) $A^{-1} = ?$

$$A^{-1} = \frac{1}{|A|} \text{Adj} [A] \text{ -----}$$

0.5 mark

$$\begin{aligned} \text{Adj} [A] &= \text{Adj} \begin{bmatrix} 1 & 7 \\ 4 & 2 \\ 2 & 2 \end{bmatrix} \\ &= \begin{bmatrix} 2 & -\frac{7}{2} \\ -2 & \frac{1}{4} \end{bmatrix} \end{aligned}$$

1 mark

put values in eq. i

$$\begin{aligned} A^{-1} &= \frac{1}{-\frac{13}{2}} \begin{bmatrix} 2 & -\frac{7}{2} \\ -2 & \frac{1}{4} \end{bmatrix} \\ &= -\frac{2}{13} \begin{bmatrix} 2 & -\frac{7}{2} \\ -2 & \frac{1}{4} \end{bmatrix} \end{aligned}$$

0.5 mark

$$\begin{aligned} &= \begin{bmatrix} -\frac{2}{13} \times 2 & -\frac{2}{13} \times -\frac{7}{2} \\ -\frac{2}{13} \times -2 & -\frac{2}{13} \times \frac{1}{4} \end{bmatrix} \\ &= \begin{bmatrix} -\frac{4}{13} & \frac{7}{13} \\ \frac{4}{13} & -\frac{1}{26} \end{bmatrix} \end{aligned}$$

1 mark

ii. Simplify using laws of exponents $\frac{(x^{m+n})^2 \times (x^{n+p})^2 \times (x^{p+m})^2}{(x^{m+n+p})^3}$

Sol.

$$= \frac{(x)^{2(m+n)} \times (x)^{2(n+p)} \times (x)^{2(p+m)}}{x^{3(m+n+p)}} \quad \because (a^m)^n = a^{mn}$$

$$= \frac{(x)^{2m+2n} \times (x)^{2n+2p} \times (x)^{2p+2m}}{(x)^{3m+3n+3p}}$$

1 mark

$$= \frac{(x)^{2m+2n+2n+2p+2p+2m}}{(x)^{3m+3n+3p}}$$

$$= \frac{x^{4m+4n+4p}}{x^{3m+3n+3p}}$$

1 mark

$$= x^{4m+4n+4p} \times x^{-(3m+3n+3p)}$$

$$= x^{4m+4n+4p} \times x^{-3m-3n-3p}$$

1 mark

$$= x^{4m+4n+4p-3m-3n-3p} \quad \because a^m \times a^n = a^{m+n}$$

$$= x^{m+n+p}$$

1 mark

iii. Simplify $\frac{2+6i}{3-i} - \frac{4-i}{3-i}$

Sol.

$$\frac{2+6i}{3-i} - \frac{4-i}{3-i}$$

$$\begin{aligned}
&= \frac{(2+6i)-(4-i)}{3-i} && \text{taking lcm} \\
&= \frac{2+6i-4+i}{3-i} \\
&= \frac{-2+7i}{3-i} && \text{1 mark} \\
&= \frac{-2+7i}{3-i} \times \frac{3+i}{3+i} && \text{by rationalizing} \\
&= \frac{-6-2i+21i+7(i^2)}{3^2-i^2} && \because (a+b)(a-b) = a^2 - b^2 \\
&= \frac{-6+19i+7(-1)}{9-(-1)} && \because i^2 = -1 \\
&= \frac{-6+19i-7}{10} && \text{1 mark} \\
&= \frac{-13+19i}{10} && \text{1 mark} \\
&= \frac{-13}{10} + \frac{19}{10}i \text{ where } a = \frac{-13}{10} \text{ and } b = \frac{19}{10} && \text{1 mark}
\end{aligned}$$

iv. If $x = \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}}$ find

- a) $\frac{1}{x}$
- b) $x + \frac{1}{x}$
- c) $x^3 + \frac{1}{x^3}$

Sol.

$$\begin{aligned}
x &= \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} \times \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} + \sqrt{3}} && \text{rationalizing} \\
x &= \frac{(\sqrt{5} + \sqrt{3})^2}{\sqrt{5}^2 - \sqrt{3}^2} && \because (a+b)(a-b) = a^2 - b^2 \quad (a+b)(a+b) = (a+b)^2 \\
x &= \frac{(\sqrt{5})^2 + (\sqrt{3})^2 + 2(\sqrt{5})(\sqrt{3})}{\sqrt{5}^2 - \sqrt{3}^2} && (a+b)^2 = a^2 + b^2 + 2ab \\
x &= \frac{5 + 3 + 2\sqrt{15}}{5 - 3} \\
x &= \frac{8 + 2\sqrt{15}}{2} \\
x &= \frac{2(4 + \sqrt{15})}{2} \\
x &= 4 + \sqrt{15} && \text{1 mark} \\
\frac{1}{x} &= \frac{1}{4 + \sqrt{15}} \\
&= \frac{1}{4 + \sqrt{15}} \times \frac{4 - \sqrt{15}}{4 - \sqrt{15}}
\end{aligned}$$

$$\begin{aligned}
&= \frac{1}{4 + \sqrt{15}} \times \frac{4 - \sqrt{15}}{4 - \sqrt{15}} \\
&= \frac{4 - \sqrt{15}}{4^2 - \sqrt{15}^2} \\
&= \frac{4 - \sqrt{15}}{16 - 15} \\
&= \frac{4 - \sqrt{15}}{1} \\
&= 4 - \sqrt{15}
\end{aligned}$$

1 mark

$$\begin{aligned}
x + \frac{1}{x} &= (4 + \sqrt{15}) + (4 - \sqrt{15}) \\
&= 4 + \sqrt{15} + 4 - \sqrt{15} \\
&= 8
\end{aligned}$$

1 mark

$$\begin{aligned}
\left(x + \frac{1}{x}\right)^3 &= x^3 + \left(\frac{1}{x}\right)^3 + 3\left(x\right)\left(\frac{1}{x}\right)\left(x + \frac{1}{x}\right) \\
(8)^3 &= x^3 + \frac{1}{x^3} + 3(8) \\
512 &= x^3 + \frac{1}{x^3} + 24 \\
512 - 24 &= x^3 + \frac{1}{x^3} \\
x^3 + \frac{1}{x^3} &= 488
\end{aligned}$$

1 mark

v. Factorize $(x+1)(x+3)(x+6)(x+8)-119$

Sol.

$$\begin{aligned}
&(x+1)(x+3)(x+6)(x+8)-119 \\
&=(x+1)(x+8)(x+3)(x+6)-119 && 0.5 \text{ mark} \\
&=(x^2+8x+x+8)(x^2+6x+3x+18)-119 \\
&=(x^2+9x+8)(x^2+9x+18)-119 && 0.5 \text{ mark} \\
\text{Let } x^2+9x &= y && 0.5 \text{ mark} \\
&=(y+8)(y+18)-119 \\
&=y^2+8y+18y+144-119 \\
&=y^2+26y+25 && 1 \text{ mark} \\
&=y^2+y+25y+25 \\
&=y(y+1)+25(y+1) \\
&=(y+1)(y+25) && 1 \text{ mark} \\
&=(x^2+9x+1)(x^2+9x+25) && 0.5 \text{ marks}
\end{aligned}$$

- vi. $f(x) = x^4 + 5x^3 - 8x^2 - 45x - 9$
- Find Remainder when $f(x)$ is divided by $(x-3)$
 - Use factor theorem to show that $(x+3)$ is a factor of $f(x)$

Sol.

a) $f(x) = x^4 + 5x^3 - 8x^2 - 45x - 9$

According to remainder theorem if a polynomial $p(x)$ is divided by $(x-a)$ then $p(a)$ is called remainder. 1 mark

So put $x=3$ in $f(x)$

$$\begin{aligned} f(3) &= 3^4 + 5(3^3) - 8(3^2) - 45(3) - 9 \\ &= 81 + 5(27) - 8(9) - 135 - 9 \\ &= 81 + 135 - 72 - 135 - 9 \\ &= 0 \end{aligned}$$

1 mark

Hence remainder is zero

a) $f(x) = x^4 + 5x^3 - 8x^2 - 45x - 9$

According to Factor theorem if a polynomial $p(x)$ is divided by $(x-a)$ and $p(a) = 0$ then $(x-a)$ is called factor of $p(x)$ 1 mark

So put $x=-3$ in $f(x)$

$$\begin{aligned} f(-3) &= (-3)^4 + 5(-3)^3 - 8(-3)^2 - 45(-3) - 9 \\ &= 81 + 5(-27) - 8(9) + 135 - 9 \\ &= 81 - 135 - 72 + 135 - 9 \\ &= 0 \end{aligned}$$

Since remainder is zero so $(x+3)$ is factor of $f(x)$

1 mark

vii. Find HCF of given polynomials by division method $3x^3 + 5x^2 - 6x - 2$; $3x^3 - 5x^2 + 6x - 4$

$$\begin{array}{r}
3x^3 - 5x^2 + 6x - 4 \quad \overline{) 3x^3 + 5x^2 - 6x - 2} \\
\underline{- \quad + \quad - \quad +} \\
10x^2 - 12x + 2 \\
2(5x^2 - 6x + 1) \quad \overline{) 3x^3 - 5x^2 + 6x - 4} \\
\underline{- \quad + \quad -} \\
15x^3 - 25x^2 + 30x - 20 \\
15x^3 - 18x^2 + 3x \\
\underline{- \quad + \quad -} \\
-7x^2 + 27x - 20 \\
x5 \\
-35x^2 + 135x - 100 \\
\underline{- \quad +} \\
-35x^2 + 42x - 7 \\
+ \quad - \quad + \\
93x - 93 \\
93(x-1) \\
x-1 \quad \overline{) 5x^2 - 6x + 1} \\
\underline{- \quad +} \\
5x^2 - 5x \\
\underline{- \quad +} \\
-x + 1 \\
-x + 1 \\
\underline{+ \quad -} \\
x
\end{array}$$

1 mark

1 mark

1 mark

HCF = $x-1$ 1 mark

viii. Find values of l and m for which the following expression become a perfect square

$$64x^4 + 153x^2 + 48x^3 + lx + m$$

Sol.

$$64x^4 + 48x^3 + 153x^2 + lx + m \quad \text{rearranging} \quad 0.5 \text{ mark}$$

$$8x^2 \overline{) \begin{array}{r} 8x^2 + 3x + 9 \\ 64x^4 + 48x^3 + 153x^2 + lx + m \\ 64x^4 \end{array}}$$

$$\underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad}$$

$$16x^2 + 3x \quad | \quad \begin{array}{r} 48x^3 + 153x^2 + lx + m \\ 48x^3 + 9x^2 \end{array} \quad 0.5 \text{ mark}$$

$$16x^2 + 6x + 9 \quad | \quad \begin{array}{r} 144x^2 + lx + m \\ 144x^2 + 54x + 81 \end{array} \quad 0.5 \text{ mark}$$

$$\underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad}$$

$$lx - 54x + m - 81$$

The given expression will be perfect square if remainder is zero

$$lx - 54x + m - 81 = 0$$

$$(l-54)x + (m-81) = 0$$

$$l-54=0$$

and

$$m-81 = 0$$

1 mark

0.5 mark

1 mark

ix. Prove that, any point on right bisector of a line segment is equidistant from its end points.

Given

A line \overline{LM} intersects the line segment AB at the point C . Such that $\overline{LM} \perp \overline{AB}$

and $\overline{AC} \cong \overline{BC}$ P is a point on \overline{LM} .

To Prove

$$\overline{PA} \cong \overline{PB}$$

Construction

Join P to the points A and B .

1 mark

Proof

Statements

In $\triangle ACP \leftrightarrow \triangle BCP$

$$\overline{AC} \cong \overline{BC}$$

$$\angle ACP \cong \angle BCP$$

$$\overline{PC} \cong \overline{PC}$$

$$\triangle ACP \cong \triangle BCP$$

$$\text{Hence } \overline{PA} \cong \overline{PB}$$

Reasons

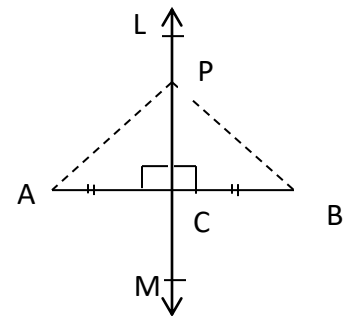
given

given $\overline{LM} \perp \overline{AB}$ so that each \angle at $C = 90^\circ$

Common

S.A.S. postulate

corresponding sides of congruent triangles



1 mark

2 mark

x. Solve for x $\frac{3|x-5|}{2} - 8 = 12 - |x-5|$

Sol.

$$\frac{3|x-5|}{2} + |x-5| = 12 + 8$$

$$|x-5| \left(\frac{3}{2} + 1 \right) = 20$$

$$|x-5| \left(\frac{3+2}{2} \right) = 20$$

1 mark

$$|x - 5| \left(\frac{5}{2}\right) = 20$$

$$|x - 5| = 20 \left(\frac{2}{5}\right)$$

$$|x - 5| = 8$$

1 mark

$$\pm(x - 5) = 8$$

$$(x - 5) = 8 \quad \text{or} \quad -(x - 5) = 8$$

$$x = 8 + 5 \quad \text{or} \quad -x + 5 = 8$$

$$x = 13 \quad \text{or} \quad -x = 8 - 5 = 3 \Rightarrow x = -3$$

1 mark

$$\text{Sol. Set} = \{13, -3\}$$

1 mark

xi. Simplify $\frac{a+b}{a^2+b^2} \cdot \frac{a}{a-b} \div \frac{(a+b)^2}{a^4-b^4}$

Sol.

$$= \frac{a+b}{a^2+b^2} \cdot \frac{a}{a-b} \times \frac{a^4-b^4}{(a+b)^2}$$

1 mark

$$= \frac{a+b}{a^2+b^2} \cdot \frac{a}{a-b} \times \frac{(a^2-b^2)(a^2+b^2)}{(a+b)(a+b)}$$

1 mark

$$= \frac{a}{a-b} \times \frac{(a+b)(a-b)}{(a+b)}$$

1 mark

$$= a$$

1 mark

xii. Evaluate $\log_{\sqrt[3]{3}} 81$ to the base $\sqrt[3]{3}$

Sol.

$$\text{Let } \log_{\sqrt[3]{3}} 81 = x$$

$$\therefore \log_a y = x \Rightarrow a^x = y$$

1 mark

$$\text{So } \log_{\sqrt[3]{3}} 81 = x$$

$$\Rightarrow (\sqrt[3]{3})^x = 81$$

1 mark

$$\Rightarrow ((3)^{\frac{1}{3}})^x = (3)^4$$

$$\Rightarrow (3)^{\frac{x}{3}} = (3)^4$$

1 mark

Bases are same exponents can be equated

$$\Rightarrow \frac{x}{3} = 4$$

$$\Rightarrow x = 3 \times 4$$

$$\Rightarrow x = 12$$

$$\text{Hence } \log_{\sqrt[3]{3}} 81 = 12$$

1 mark

xiii. Find the values of x and y for the given congruent triangles

Sol.

$$\Delta RSU \cong \Delta RUT \quad \text{Given}$$

$$m \angle T = m \angle S$$

$$(5x + 5)^\circ = 50^\circ$$

1 mark

$$5x = 50 - 5$$

$$5x = 45$$

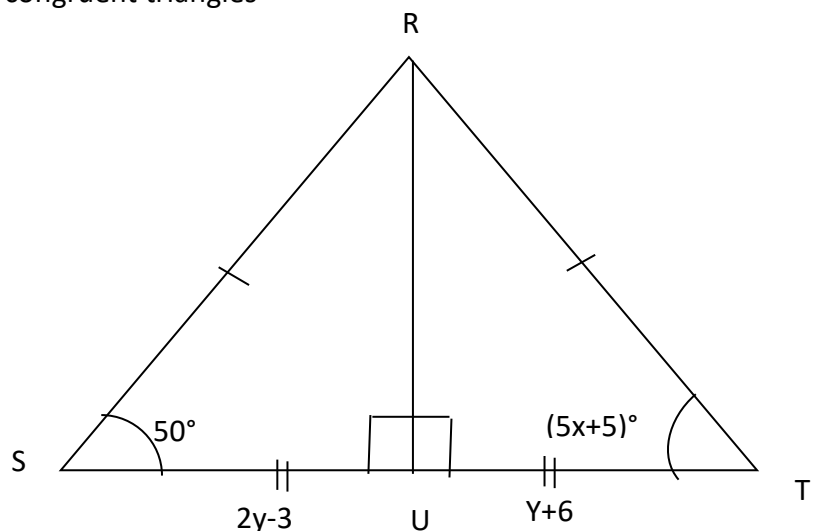
$$x = 45/5$$

$$x = 9^\circ$$

1 mark

also

$$SU = UT$$



$$2y-3 = y + 6 \quad 1 \text{ mark}$$

$$2y-y = 6+3$$

$$y = 9 \quad 1 \text{ mark}$$

Xiv. Given

$$m\overline{AB} = 5 \text{ cm,}$$

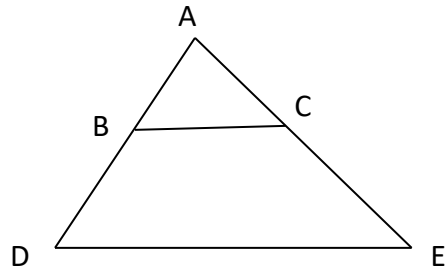
$$m\overline{BD} = 10 \text{ cm}$$

$$m\overline{AE} = 18 \text{ cm,}$$

$$\overline{BC} \parallel \overline{DE}$$

To find

$$m\overline{AC} = ?$$



Sol.

$$\overline{BC} \parallel \overline{DE}$$

$$\frac{m\overline{AB}}{m\overline{AD}} = \frac{m\overline{AC}}{m\overline{AE}} \quad \text{-----i)}$$

1 mark

$$m\overline{AD} = m\overline{AB} + m\overline{DB}$$

$$m\overline{AD} = 5 + 10$$

$$m\overline{AD} = 15$$

1 mark

Put values in eq. i)

$$\frac{5}{15} = \frac{m\overline{AC}}{18}$$

1 mark

$$15 m\overline{AC} = 5 \times 18$$

$$m\overline{AC} = \frac{90}{15}$$

$$m\overline{AC} = 6 \text{ cm}$$

1 mark

Section C (8x3=24)

Q no 3:

Part a) L.H.S= $(AB)^t$

$$AB = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix} \begin{bmatrix} 5 & 7 \\ 6 & 8 \end{bmatrix}$$

$$= \begin{bmatrix} (1)(5) + (3)(6) & (1)(7) + (3)(8) \\ (2)(5) + (4)(6) & (2)(7) + (4)(8) \end{bmatrix}$$

$$= \begin{bmatrix} 23 & 31 \\ 34 & 46 \end{bmatrix}$$

L.H.S= $(AB)^t$

$$= \begin{bmatrix} 23 & 31 \\ 34 & 46 \end{bmatrix}^t$$

$$= \begin{bmatrix} 23 & 34 \\ 31 & 46 \end{bmatrix} \text{-----eq(1)}$$

Now R.H.S= $B^t A^t$

$$B^t = \begin{bmatrix} 5 & 7 \\ 6 & 8 \end{bmatrix}^t$$

$$= \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix}$$

$$A^t = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}^t$$

$$= \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

R.H.S= $B^t A^t$

$$= \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$= \begin{bmatrix} (5)(1) + (6)(3) & (5)(2) + (6)(4) \\ (7)(1) + (8)(3) & (7)(2) + (8)(4) \end{bmatrix}$$

$$= \begin{bmatrix} 23 & 34 \\ 31 & 46 \end{bmatrix} \text{-----eq(2)}$$

From eq(1) and eq(2) L.H.S=R.H.S

Q No 3:

Part b:

$$A^{-1} = \frac{adj A}{|A|}$$

$$|A| = \begin{vmatrix} 1 & 3 \\ 2 & 4 \end{vmatrix}$$

$$= (1)(4) - (3)(2)$$

$$= -2$$

$$adj A = \begin{bmatrix} 4 & -3 \\ -2 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{\begin{bmatrix} 4 & -3 \\ -2 & 1 \end{bmatrix}}{-2}$$

$$= \begin{bmatrix} \frac{4}{-2} & \frac{-3}{-2} \\ \frac{-2}{-2} & \frac{1}{-2} \end{bmatrix}$$

$$= \begin{bmatrix} -2 & \frac{3}{2} \\ 1 & \frac{-1}{2} \end{bmatrix}$$

$$L.H.S = A.A^{-1}$$

$$= \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix} \begin{bmatrix} -2 & \frac{3}{2} \\ 1 & \frac{-1}{2} \end{bmatrix}$$

$$= \begin{bmatrix} -2 + 3 & \frac{3}{2} - \frac{3}{2} \\ -4 + 4 & 3 - 2 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \text{-----eq(3)}$$

$$R.H.S = A^{-1}.A$$

$$= \begin{bmatrix} -2 & \frac{3}{2} \\ 1 & \frac{-1}{2} \end{bmatrix} \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$$

$$= \begin{bmatrix} -2 + 3 & -6 + 6 \\ 1 - 1 & 3 - 2 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \text{-----eq(4)}$$

From eq(3) and eq(4)

$$L.H.S = R.H.S$$

Q No 4:

Given: ΔABC is a right angled triangle in which $m \angle C = 90^\circ$ and $\overline{BC} = a$,

$m\overline{AC} = b$ and $m\overline{AB} = c$.

To Prove:

$$c^2 = a^2 + b^2$$

Construction:

Draw \overline{CD} perpendicular from C on \overline{AB} .

;

Let $m\overline{CD} = h$, $m\overline{AD} = x$ and $m\overline{BD} = y$. Line segment CD splits ΔABC into two

Δs ADC and BDC which are separately shown in the figures (ii)-a and (ii)-b

Respectively.

Proof (Using similar Δs)

	Statements	Reasons
In	$\Delta ADC \leftrightarrow \Delta ACB$ $\angle A \cong \angle A$ $\angle ADC \cong \angle ACB$ $\angle C \cong \angle B$ $\therefore \Delta ADC \sim \Delta ACB$ $\therefore \frac{x}{b} = \frac{b}{c}$	Refer to figures (ii)-a and (i) Common-self congruent Construction – given, each angle = 90° $\angle C$ and $\angle B$, complements of $\angle A$ Congruency of three angles Measures of corresponding sides of similar triangles are proportional
Or	$x = \frac{b^2}{c}$(I)	
Again in	$\Delta BDC \leftrightarrow \Delta BCA$ $\angle B \cong \angle B$ $\angle BDC \cong \angle BCA$ $\angle C \cong \angle A$ $\therefore \Delta BDC \sim \Delta BCA$ $\therefore \frac{y}{a} = \frac{a}{c}$	Refer to fig(ii)-b and (i) Common-self congruent Construction-given, each angle = 90° $\angle C$ and $\angle A$, complements of $\angle B$ Congruency of three angles
Or	$y = \frac{a^2}{c}$(II)	Supposition
But	$y + x = c$	By (I) and (II)
	$\therefore \frac{a^2}{c} + \frac{b^2}{c} = c$	
Or	$a^2 + b^2 = c^2$	

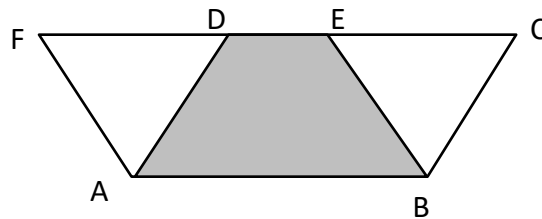
Q 6.
 Prove that parallelograms on the same base between the same parallel lines (or of same altitude) are equal in area.

Given:

Two parallelograms $ABCD$ and $ABEF$ having the same base \overline{AB} and between the same parallel lines \overline{AB} and \overline{DE} .

To prove:

Area of parallelogram $ABCD$ = Area of parallelogram $ABEF$



Proof:

Statements	Reasons
Area of parallelogram ABCD= area of quad ABED + area of ΔCBE -----i	Area addition axiom
Area of parallelogram ABEF= area of quad ABED + area of ΔDAF -----ii	Area addition axiom
In $\Delta CBE \leftrightarrow \Delta DAF$	
$m\overline{CB} = m\overline{DA}$	Opposite sides of parallelogram
$m\overline{BE} = m\overline{AF}$	Opposite sides of parallelogram
$m\angle CBE = m\angle DAF$	$\overline{BC} \parallel \overline{AD}$ and $\overline{BE} \parallel \overline{AF}$
$\Delta CBE \cong \Delta DAF$	S.A.S congruent axiom
area of $\Delta CBE =$ area of ΔDAFiii	Congruent area axiom
Hence Area of parallelogram ABCD =Area of parallelogram ABEF	From eq. I, eq. ii and eq. iii

Q.7.
Find b such that the points A(2, b) , B(5, 5) and C(-6, 0) are the vertices of right angle triangle ABC with $m\angle BAC = 90^\circ$

Sol.
Given
A(2, b) , B(5, 5) and C(-6, 0)
 ΔABC is right angle triangle
 $m\angle BAC = 90^\circ$

To find
B=?

Distance Formula:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2$$

$$|AB|^2 = (5-2)^2 + (5-b)^2$$

$$= (3)^2 + (5-b)^2$$

$$|AB|^2 = 9 + (5-b)^2 \text{-----1}$$

$$|BC|^2 = (-6-5)^2 + (5-0)^2$$

$$= (-11)^2 + (5)^2$$

$$= 121 + 25$$

$$|BC|^2 = 146 \text{-----2}$$

$$|AC|^2 = (-6-2)^2 + (b-0)^2$$

$$= (-8)^2 + (b)^2$$

$$|AC|^2 = 64 + b^2 \text{-----3}$$

According to Pythagoras Theorem

$$|BC|^2 = |AB|^2 + |AC|^2$$

$$146 = (3)^2 + (5-b)^2 + 64 + b^2$$

$$146 = 9 + 5^2 + b^2 - 10b + 64 + b^2$$

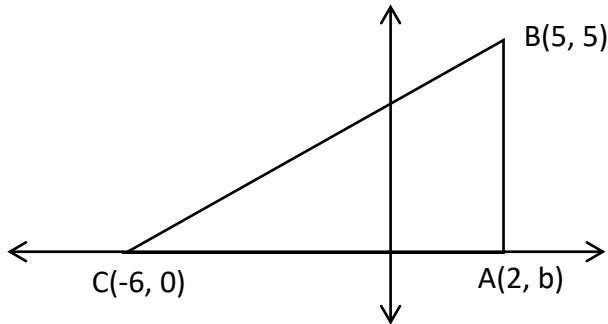
$$146 = 9 + 25 + 64 + b^2 + b^2 - 10b$$

$$146 = 98 + 2b^2 - 10b$$

$$2b^2 - 10b + 98 - 146 = 0$$

$$2b^2 - 10b - 48 = 0$$

$$2(b^2 - 5b - 24) = 0$$



2 marks

1 mark

1 mark

1 mark

from eq. 1, eq. 2 and eq. 3

$$(a-b)^2 = a^2 + b^2 - 2ab$$

1 mark

$$b^2 - 5b - 24 = 0$$

1 mark

$$b^2 - 5b - 24 = 0$$

$$b^2 - 8b + 3b - 24 = 0$$

$$b(b-8) + 3(b-8) = 0$$

$$(b-8)(b+3) = 0$$

$$b-8=0 \text{ or } b+3=0$$

$$b=8 \text{ or } b=-3$$

1 mark

Q. 7

If $\overline{mZX} = 5 \text{ cm}$, $m\angle X = 75^\circ$ and $m\angle Y = 45^\circ$

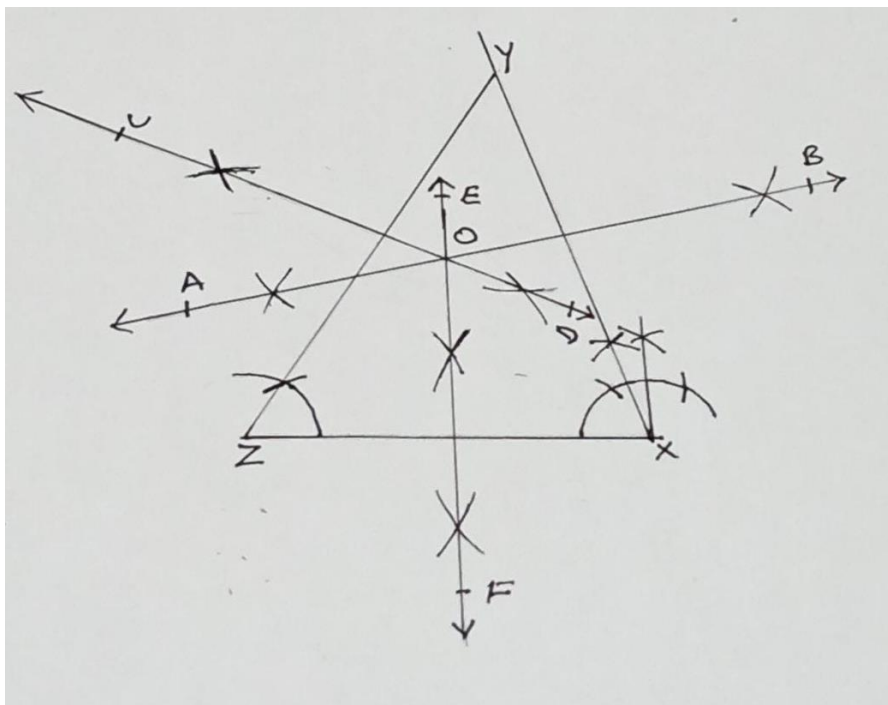
- Construct triangle XYZ
- Draw perpendicular bisectors of the three sides of ΔXYZ
- Are the perpendicular bisectors concurrent.

Given

$\overline{mZX} = 5 \text{ cm}$, $m\angle X = 75^\circ$ and $m\angle Y = 45^\circ$

Required:

- Construct triangle XYZ
- Draw perpendicular bisectors of the three sides of ΔXYZ
- Are the perpendicular bisectors concurrent.



3 marks

Steps of construction:

Part a.

- Draw the line segment $\overline{mZX} = 5 \text{ cm}$
- At the end point X of ZX make $m\angle X = 75^\circ$
- $m\angle X + m\angle Y + m\angle Z = 180^\circ$

$$75^\circ + 45^\circ + m + \angle Z = 180^\circ$$

$$m + \angle Z = 180^\circ - 75^\circ - 45^\circ$$

$$m + \angle Z = 60^\circ$$

$$\text{At } Z \text{ make } m + \angle Z = 60^\circ$$

4. Arms of $\angle X$ and $\angle Z$ intersect at point Y. $\triangle XYZ$ is required triangle. 3 marks

Part b.

Draw perpendicular bisectors \overleftrightarrow{AB} , \overleftrightarrow{CD} , \overleftrightarrow{EF} , of the sides \overline{XY} , \overline{YZ} and \overline{ZX} respectively. 1 mark

Part c.

Yes the perpendicular bisectors are concurrent at O. 1 mark